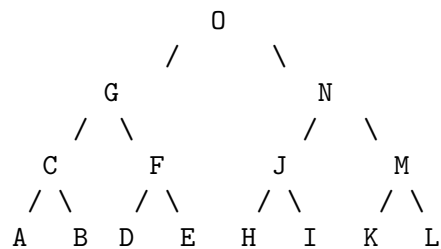


1. (a) This is actually bubble sort. The outer loop iterates n times, the inner loop on average $n/2$ times, so asymptotic complexity $\Theta(n^2)$. It is an in-place sorting algorithm.
- (b) Use the Master Theorem, with $a = 8$ and $b = 2$, so $E = \log 8 / \log 2 = 3$. $f(n) \in \Theta(n^3)$ holds, so this is condition 2, so $T(n) \in \Theta(n^3 \log(n))$.
2. (a) A is already a maxheap, so do nothing: complexity $\Theta(0)$.
- (b) The tree is



If you traverse this tree in a pre-order way you encounter the letters in the order OGCABFDENJHIMKL.

- (a) If you arrive in square (i, j) then the optimal number number of pearls is $c(i, j)$ plus the maximum of the pearls from where you come from, so the maximum of $P(i-1, j)$ and $P(i, j-1)$. So the right answer is ii.
- (b) `def maxpoints(c,n):`

```

P=[[0 for j in range(n+1)] for i in range(n+1)]

for i in range(1,n+1):
    for j in range(1,n+1):
        P[i][j] = max(P[i-1][j],P[i][j-1]) + c[i][j]

return P[n][n]

```

The complexity of this algorithm is $\Theta(n^2)$.