```
import Data.List
import Test.QuickCheck
```

-- For general grading criteria, see the last two pages of the PDF
-- Question 1
myscanl :: (b -> a -> b) -> b -> [a] -> [b]
myscanl fy [] = y : []
myscanl $f y(x: x s)=y$ : myscanl f (f y x) xs
prop_myscanl :: Integer -> [Integer] -> Bool
prop_myscanl x xs = myscanl (-) x xs == scanl (-) x xs
-- Note:
-- the type must be generic (not limited to numbers only)
-- Question 2
cycle' :: [a] -> [a]
cycle' xs = [ x | $\mathrm{y}<-[1 .],. \mathrm{x}<-\mathrm{xs}]$
prop_cycle :: Small Int -> NonEmptyList Integer -> Bool
prop_cycle (Small n) (NonEmpty xs) = take $n$ (cycle xs) == take $n$ (cycle' xs)
-- Question 3
find' :: (a -> Bool) -> [a] -> Maybe a find' $f=$ foldr ( $\backslash x$ y -> if $f x$ then (Just $x$ ) else y) Nothing
prop_find $x s=$ find $(<\theta) \times s==f^{\prime}{ }^{\prime}(<\theta) \times s$
-- Question 4
zipFiles :: FilePath -> FilePath -> IO [(String, String)] zipFiles f1 f2 = zip <\$> (lines <\$> readFile f1) <*> (lines <\$> readFile f2)

```
-- Question 5
```

```
maximum' :: Ord a => [a] -> a
maximum' = head . reverse . sort
prop_maximum :: NonEmptyList Integer -> Bool
prop_maximum (NonEmpty xs)= maximum xs == maximum' xs
-- Question 6
```

mzip :: [Maybe a] -> [Maybe b] -> [(a,b)]

```
mzip :: [Maybe a] -> [Maybe b] -> [(a,b)]
mzip _ [] = []
mzip _ [] = []
mzip [] _ = []
mzip [] _ = []
mzip (Just x:xs) (Just y:ys) = (x,y) : mzip xs ys
mzip (Just x:xs) (Just y:ys) = (x,y) : mzip xs ys
mzip (x:xs) (y:ys) = mzip xs ys
mzip (x:xs) (y:ys) = mzip xs ys
-- Question 7
-- Question 7
-- a
-- a
data Tree a = Node a (Tree a) (Tree a)
data Tree a = Node a (Tree a) (Tree a)
    | Leaf
    | Leaf
    deriving (Show, Eq, Ord)
    deriving (Show, Eq, Ord)
-- b
treeins :: Ord a => a -> Tree a -> Tree a
treeins x (Node a t1 t2) | x < a = Node a (treeins x t1) t2
    | otherwise = Node a t1 (treeins x t2)
treeins x Leaf = Node x Leaf Leaf
```

-- C
list2tree : : Ord a => [a] -> Tree a
list2tree xs = foldr treeins Leaf xs
-- d
tree2list Leaf = []
tree2list (Node x t1 t2) = tree2list t1 ++ [x] ++ tree2list t2
-- e
listsort : : Ord a => [a] -> [a]
listsort = tree2list . list2tree

```
prop_listsort :: [Int] -> Bool
prop_listsort xs = listsort xs == sort xs
-- Question 8
-- a
data Stream a = Stream a (Stream a)
-- b
toList (Stream x xs) = x : toList xs
-- c
instance Functor Stream where
    fmap f (Stream x xs) = Stream (f x) (fmap f xs)
-- d
-- No: as a consequence of the Functor laws, Functors are uniquely
defined
-- (on the exam, we expect compact answers)
-- e
instance Applicative Stream where
    pure x = Stream x (pure x)
    (Stream f fs) <*> (Stream x xs) = Stream (f x) (fs <*> xs)
-- f
zipstream :: Stream a -> Stream b -> Stream (a,b)
zipstream x y = (,) <$> x <*> y
-- Question 9
ones = 1 : ones
r = 1 : zipWith (+) r ones
```

